

REPORT DOCUMENTATION PAGE			Form Approved OMB No. 0704-0188	
Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project (0704-0188), Washington, DC 20503.				
1. AGENCY USE ONLY (Leave blank)	2. REPORT DATE December 6, 2000	3. REPORT TYPE AND DATES COVERED Final Report, 8/1/1996-7/31/1999		
4. TITLE AND SUBTITLE Hierarchical Modeling and Simulation Techniques with Application to Computational Fluid Dynamics and Fluid-Flow Control		5. FUNDING NUMBERS  G: F49620-96-0327		
6. AUTHORS C.R. Anderson and J.S. Gibson		8. PERFORMING ORGANIZATION REPORT NUMBER		
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) Mathematics Department 7619B Math Sciences Building University of California, Los Angeles Los Angeles, CA 90095-1555		10. SPONSORING/MONITORING AGENCY REPORT NUMBER		
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES) AFOSR/NA 801 N. Randolph Street, Room 732 Arlington, VA 22203-1977		11. SUPPLEMENTARY NOTES The views, opinions and/or findings contained in this report are those of the author(s) and should not be construed as an official Department of the Air Force position, policy or decision, unless so designated by other documentation.		
12a. DISTRIBUTION/AVAILABILITY STATEMENT  Approved for public release; distribution unlimited		12b. DISTRIBUTION CODE  UL		
13. ABSTRACT (Maximum 200 words)  The primary research objective of this contract was to investigate and develop fluid flow control procedures by utilizing a hierarchical modeling approach. This project included research on control and identification methods for vortex wakes, with the primary example being stabilization of vortices behind a flat plate. Vortex blob and finite difference methods were constructed to provide the flow dynamics. Linear time-invariant feedback controllers have been developed, as well as identification results for a class of input/output models that can be used to design more sophisticated controllers. Additionally, Java based software components that support hierarchical modeling efforts were created.				
14. SUBJECT TERMS fluid flow control, vortex wakes, feedback control, identification, computational mathematical models			15. NUMBER OF PAGES 7	
			16. PRICE CODE	
17. SECURITY CLASSIFICATION OF REPORT Unclassified	18. SECURITY CLASSIFICATION OF THIS PAGE Unclassified	19. SECURITY CLASSIFICATION OF ABSTRACT Unclassified	20. LIMITATION OF ABSTRACT  UL	

NSN 7540-01-280-5500

Computer Generated

STANDARD FORM 298 (Rev 2-89)  
Prescribed by ANSI Std Z39-18  
298-102

DTIC QUALITY INSPECTED 4

20001227 029



MECHANICAL AND AEROSPACE ENGINEERING DEPARTMENT  
SCHOOL OF ENGINEERING AND APPLIED SCIENCE  
420 WESTWOOD PLAZA  
BOX 951597  
LOS ANGELES, CALIFORNIA 90095-1597

FAX: (310) 206-4830

DTIC-OCP  
8725 John J Kingman Road, Suite 0944  
Fort Belvoir VA 22060-6218

Ladies and Gentlemen:

Enclosed please find two copies of the final technical reports for the following AFOSR grants:

F49620-96-1-0327  
F49620-97-1-0132.

These reports have been approved by the AFOSR technical monitor, Dr. Marc Q. Jacobs, at AFOSR/NA.

Sincerely,

J.S. Gibson  
Professor of Engineering  
and Applied Science

cc: AFOSR/PKA  
UCLA - Office of Contract & Grant Admin.

JLS:cg

# Hierarchical Modeling and Simulation Techniques with Application to Computational Fluid Dynamics and Fluid-Flow Control

AFOSR F-49620-96-1-0327

## Final Report

C.R. Anderson  
Department of Mathematics  
University of California, Los Angeles  
90095-1555

J.S. Gibson  
Mechanical and Aerospace Engineering  
University of California, Los Angeles  
90095-1597

### Executive Summary

The primary research objective of this contract was to investigate and develop fluid flow control procedures by utilizing a hierarchical modeling approach. Constituent tasks were

- The creation of a hierarchy of mathematical models (and their computational implementation) for the simulation of vortex shedding phenomena.
- Development of adaptive identification and control procedures appropriate for problems involving vortex shedding.
- Development and implementation of a software infrastructure suitable for hierarchical modeling efforts.

This project included research on control and identification methods for vortex wakes, with the primary example being stabilization of vortices behind a flat plate. Vortex blob and finite difference methods were constructed to provide the flow dynamics. Linear time-invariant feedback controllers have been developed, as well as identification results for a class of input/output models that can be used to design more sophisticated controllers. Additionally, Java based software components that support hierarchical modeling efforts were created. The results of this research have been presented in publications and reports [1] - [14].

### Personnel Supported

Faculty : Prof. J.S. Gibson, Prof. C.R. Anderson

Post-Doc : Yen-Cheng Chen

Graduate Students : Rachel Caiden

Other : Mark Hoefer, Tyler Quoc Dinh (UCLA undergraduates).

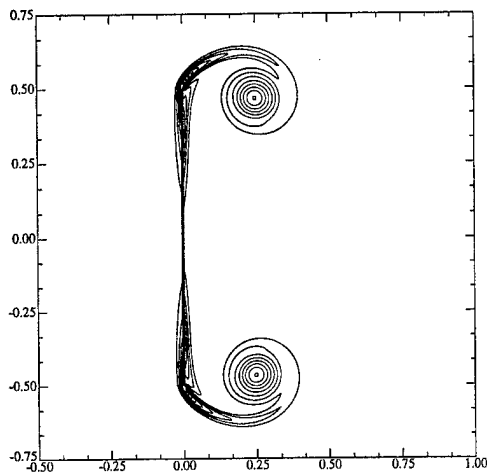


Figure 1(a). Vorticity distribution for flow past a flat plate (finite difference method).

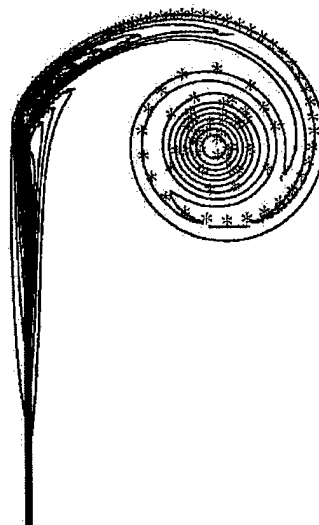


Figure 1(b). Vortex Method/Finite Difference Method Comparison

## Results Summaries

### Hierarchical Modeling

The flow dynamics of our target control problem were modeled using a vortex blob method. In this method the evolution of the vorticity in the wake is approximated by evolving a collection of discrete vortices. The vortex shedding phenomenon (the principal viscous effect) is modeled by employing a dynamic Kutta condition. As discussed in a number of previous papers [15, 16, 18, 19] vortex methods provide a description of the dynamics as a model with far fewer dimensions than direct numerical simulation. This reduced dimensionality makes vortex methods particularly attractive as simulations to supply approximate dynamics for the task of developing identification and control procedures. However, in order to make the vortex model suitable for identification and control, it was necessary to modify the standard discrete vortex method. Modifications discussed in [1, 3] include an adaptive time-stepping scheme, vortex merging, and a procedure for reducing the noise in velocity measurements near the body.

Another part of the hierarchical modeling effort consisted of constructing a finite difference method that computed the two-dimensional flow about a flat plate (this method is used to validate the vortex model). A major difficulty in creating this method was the proper treatment of the infinite extent of the domain. Previously this problem had been dealt with by employing a finite difference version of the panel method — i.e. one uses velocity field basis elements that are appropriate for an infinite domain. In such a technique one must solve a linear system of equations that is a discrete version of a first-kind integral equation. This procedure has the unsatisfactory property that as the mesh is refined the solution of the linear system becomes more and more difficult to obtain — effectively limiting the resolution that can be employed. In [13] an infinite domain “projection method” was developed that overcomes this problem, thus allowing us to compute solutions of the Navier-Stokes equation in infinite domains without compromising accuracy. Sample results of this calculation are presented in Figure 1(a)-(b).

In addition, work on finite difference methods that simulate the motion of a fluid with large density ratios (such as that occurring in the combustion of fuel droplets) was carried out. In the procedure developed, the fluid was treated as a mixture of compressible and incompressible fluids with numerical methods appropriate for each type of fluid being employed. By utilizing a compressible/incompressible approach,

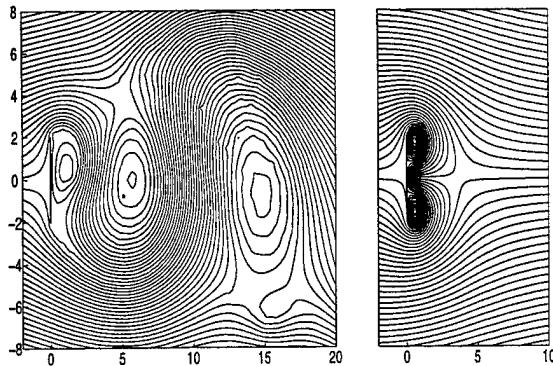


Figure 2. Instantaneous streamlines for flow past a flat plate (vortex method).

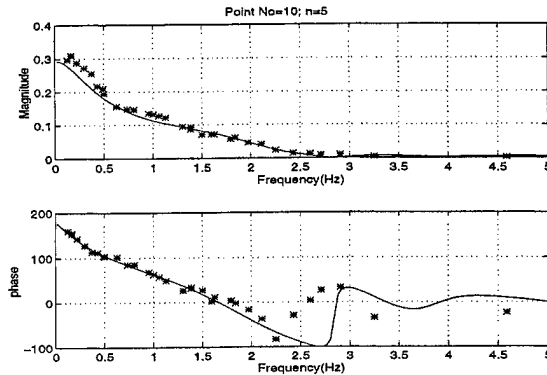


Figure 3. Bode plots for the vortex simulation (\*) and the identified ARX model of order 5 (solid lines)

problems that occur when treating the fluid as a single compressible fluid were avoided (e.g. the severe timestep restriction). Aspects of the work included the development of appropriate boundary conditions at the compressible/incompressible interface and extension of level set method techniques to the problem of evolving a compressible/incompressible interface. Details of the procedure are described in [14].

## Research on Flow Control

Our research on control and identification methods for vortex wakes are presented in [1, 2, 3]. This work concerns the stabilization of vortices behind a flat plate, using backside suction as an actuator. The flow dynamics are modeled with a discrete vortex method. Feedback control results for a linear PI controller are presented as well as identification results for a class of input/output models that can be used to design more sophisticated controllers.

In the case of constant free-stream velocity, vortex shedding occurs and a vortex wake forms behind the plate. Our results demonstrate the feasibility of using feedback control in this problem by applying a constant-gain linear feedback to trap the vortices and inhibit shedding when there is no disturbance to the flow field. Most real flow-control applications involve time-varying free-stream velocities and unmodeled disturbances, and these will require more sophisticated controllers. Hence, our research also has investigated the identification of input/output models that can be used to design such controllers.

Our results illustrate that with appropriate modifications, discrete-vortex models can be quite useful for control design and simulation. In particular, the agreement found between the discrete-vortex model and the identified input/output model with respect to the minimum phase and nonminimum phase characteristics of the flow field indicates that the identified input/output models obtained from the discrete-vortex model capture the characteristics of the flow that are important in control system design.

The uncontrolled flow past the plate is shown in Figure 2(a) and is characterized by the formation of vortex street. The vortex shedding causes unsteady drag forces to be exerted upon the plate. In an effort to reduce these unsteady forces, the control problem becomes one of trying to trap the vortices behind the plate and thus inhibit the vortex shedding process. Suction on the centerline of the downstream side of the plate is used as an actuator.

The possibility that the vortices can be trapped and vortex shedding inhibited is demonstrated in Figure 2(b), where we show the results of applying an open-loop constant control. In general, the amount of suction necessary to trap the vortices when there is non-constant free stream velocity and/or unmodeled disturbances is not known, therefore closed-loop control strategies capable of determining the appropriate suction are desired.

For design of adaptive and other sophisticated controllers, an input/output model must be identified. The full dynamics of the flow are too nonlinear to be represented by a single linear input/output model, so we

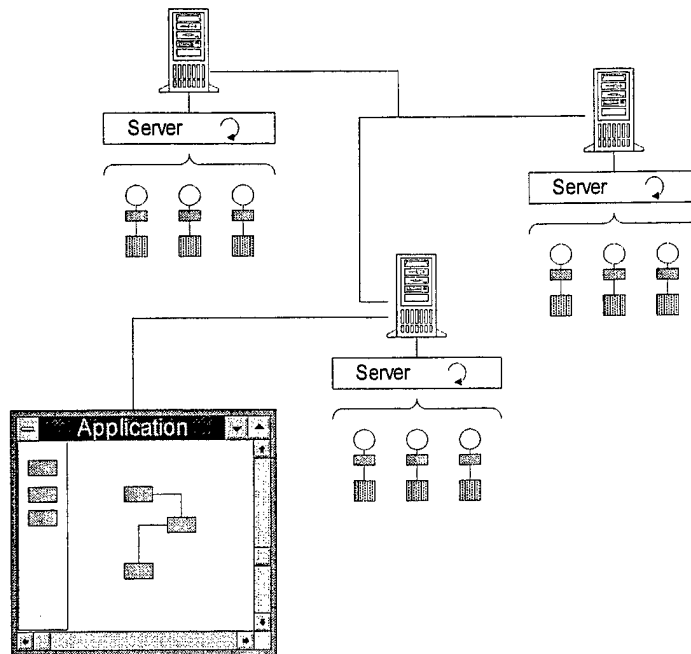


Figure 4. Distributed application structure

chose to identify a linear input/output model of the vortex dynamics for perturbations from a nominal steady-state flow. The identified discrete-time input/output model has the form of the ARX (auto-regressive with exogenous input) model. The measurements used for system identification are point velocity measurements on the downstream side of the plate.

Typical results of the system identification are shown in Figure 3. Amplitude and phase responses corresponding to single-frequency inputs are shown by asterisks. The amplitude matches very well, and the phase matches very well at low frequency. At frequencies around half the Nyquist frequency, the phase shows significant errors. However, because the amplitude is very small in this frequency range, these phase errors do not represent a significant difference between the frequency response of the vortex simulation and the frequency response of the ARX model.

## Software Infrastructure

A primary research objective of this contract was to investigate and develop fluid flow control procedures by utilizing a hierarchical modeling approach. To achieve this goal required that we construct simulations that were combinations of control codes, fluid simulation codes, and visualization/input-output codes. Many of the codes were written in different languages and were functional on different types of machines. (e.g. Unix workstations and PC's). The problem was to figure out a way that simulations could be created without rewriting component codes and without having to port all the codes to a single computational platform.

Our solution to this problem consisted of developing a software infrastructure that supported the creation of distributed applications; e.g. applications in which individual components exist on separate machines and communicate over a network. This solution avoids the cost of rewriting codes, since the construction of the distributed application only requires that the component codes be "wrapped" with code that enables them to be managed by a distributed application server. In addition, the component codes can remain on the machine that they were developed thus avoiding the cost of porting codes to a single platform.

Our software infrastructure was constructed using the Java programming language. To create distrib-

uted applications requires software that allows components residing on remote machines to be managed — dynamically loading components, establishing communication links, and controlling execution. The JAVA package *cam.netapp* was created to provide this capability. A report [4] as well as documentation [5] and source [6] are available on the Web. Additionally, to use this Java infrastructure with C, C++ or Fortran codes requires that one interface Java to these codes. While not particularly difficult, there are technical details that are useful to know, and these are discussed in [7]; also available on the Web.

After some experimentation with this infrastructure, it became apparent that getting component codes into a form that allowed them to be integrated into a distributed application requires a considerable amount of tedious programming. As described in [8], creating distributed applications should be as easy as creating web pages that have links to remote pages. To reduce the time it takes to create distributed applications, we automated the process of programming the “wrappers” for the component codes. The description of this process is described in [9], with source and documentation available in [10] and [11].

During the contract, C. Anderson was co-organizer of a workshop concentrating on software issues in scientific technical computing. Proceedings of this workshop have been published [12].

## Publications and Reports

- [1] Y.-C. Chen, *Control and Identification of the Flow Past a Flat Plate with Discrete Vortex Simulations*. PhD thesis, University of California, Los Angeles, 1997.
- [2] C. R. Anderson, Y.-C. Chen, and J. S. Gibson, “Control and identification of vortex wakes,” in *ASME Fluids Engineering Division Summer Meeting*, ASME, June 1998.
- [3] C. R. Anderson, Y.-C. Chen, and J. S. Gibson, “Control and identification of vortex wakes,” *ASME Journal of Dynamic Systems, Measurement, and Control*, vol. 122, pp. 298–305, June 2000.
- [4] C.R. Anderson, *Creating Distributed Applications In Java Using cam.netapp Classes*, Sept. 1998, CAM Report 98-39, or <http://www.math.ucla.edu/~anderson/JAVAcass/JavaDistributed/index.html>
- [5] C.R. Anderson, *Java package cam.netapp : Documentation*, 1998, <http://www.math.ucla.edu/~anderson/JAVAcass/cam/netapp/NetAppDoc.html>
- [6] C.R. Anderson, *Java package cam.netapp : Source Code*, 1998, <http://www.math.ucla.edu/~anderson/JAVAcass/CAMJavaPackageSource.html>
- [7] C.R. Anderson, *Putting a Java Interface on you C, C++ or Fortran Code*, July 1997, <http://www.math.ucla.edu/~anderson/JAVAcass/JavaInterface/JavaInterface.html>
- [8] C.R. Anderson “Distributed Computing : What do we need and can we get it with Java?” Proceedings of the “SIAM Workshop on Object Oriented Methods for Inter-operable Scientific and Engineering Computing” October 21-23, 1998, IBM TJ Watson Research Center, Yorktown Heights, New York SIAM Publications, (1999)
- [9] C.R. Anderson, *NetApp Wrappers : Higher level construction of distributed applications using the cam.netapp package*, Sept. 1998, CAM Report 98-39, or <http://www.math.ucla.edu/~anderson/JAVAcass/NetAppWrappers/NetAppWrap.html>
- [10] C.R. Anderson, *Java package cam.codegen : Source Code*, 1998, <http://www.math.ucla.edu/~anderson/JAVAcass/CAMJavaPackageSource.html>
- [11] C.R. Anderson, *Java package cam.codegen : Documentation*, 1998, <http://www.math.ucla.edu/~anderson/JAVAcass/cam/codegen/CodeGen.html>

- [12] M. Henderson, C.R. Anderson, S.Lyons, "Object Oriented Methods for Inter-operable Scientific and Engineering Computing", Conference Proceedings for SIAM Workshop held at IBM T.J. Watson Research Center, Yorktown Heights, NY, Oct 1998. SIAM Publications.
- [13] C.R. Anderson, *Numerical Solution of the Incompressible Navier-Stokes Equations in Infinite Domains*, Jan. 2000, CAM Report 00-02.
- [14] R.C. Caiden, R.P. Fedkiw, C.R. Anderson, *A Numerical Method for Two Phase Flow Consisting of Separate Compressible and Incompressible Regions*, J. Comput. Phys. (in press 2000).

## Additional References

- [15] L. Cortelezzi, *A Theoretical and Computational Study on Active Wake Control*. PhD thesis, California Institute of Technology, 1993.
- [16] L. Cortelezzi, *Nonlinear Feedback Control of the Wake Past a Plate with a Suction Point on the Downstream Wall*. Journal of Fluid Mechanics, Vol. 327, 303–324.
- [17] L. Cortelezzi, Y.-C. Chen, and H.-L. Chang, *Nonlinear Feedback Control of the Wake Past a Plate: from a Low-order Model to a Higher-order Model*. Physics of Fluids A, Vol. 9, (7), 2009–2022.
- [18] Turgut Sarpkaya, *An inviscid model of two-dimensional vortex shedding for transient and asymptotically steady separated flow over an inclined plate*. Journal of Fluid Mechanics, 68:109–128, 1975.
- [19] Turgut Sarpkaya, and Ray L. Schoaff, *Inviscid model of two dimensional vortex shedding by a circular cylinder*. AIAA Journal, 17(11): 1193–1200, 1979.